

# TRANSFORMATIONS

**RIGID**  
leave the size & shape of a graph unchanged

**Absolute Value**

**NON-RIGID**  
usually distort the shape of a graph

Horizontal

Vertical

- $y = f(x-c)$   
translation to the right by  $c$  units
- $y = f(x+c)$   
translation to the left by  $c$  units

- $y = f(x)+c$   
translation up by  $c$  units
- $y = f(x)-c$   
translation down by  $c$  units

$f(|x|)$

- all  $x$  values become (+)
- keep the right side
- delete left side, reflect right side across  $y$ -axis

$|f(x)|$

- all  $y$  values become (+)
- keep the top & reflect the bottom across  $x$ -axis

**REFLECTIONS**

- $y = -f(x)$   
reflection across  $x$ -axis
- $y = f(-x)$   
reflection across  $y$ -axis

Horizontal stretches/shrinks  
 $y = f\left(\frac{x}{c}\right)$

- a stretch by a factor of  $c$  if  $c > 1$
- a shrink by a factor of  $c$  if  $c < 1$

Vertical stretches/shrinks  
 $y = c \cdot f(x)$

- a stretch by a factor of  $c$  if  $c > 1$
- a shrink by a factor of  $c$  if  $c < 1$